

# Clark School Engineering Solutions for COVID-19

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**Balakumar Balachandran, Ph.D.**

Department Chair, Mechanical Engineering

Minta Martin Professor

Faculty Member, Applied Mathematics and Scientific Computation

[balab@umd.edu](mailto:balab@umd.edu)

**Relevant Expertise:**

Data-Driven Approaches and Forecasting, Delay Systems,  
Nonlinear Dynamics, System Identification



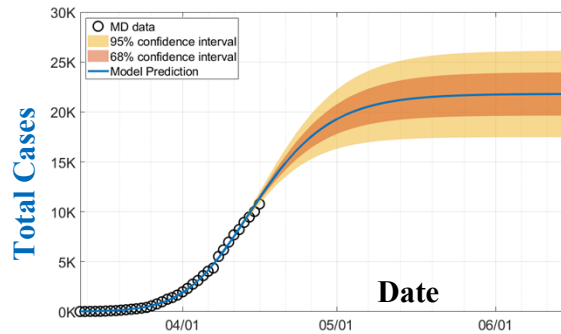
**Website(s):**

[//enme.umd.edu/research/institutes-labs-centers](https://enme.umd.edu/research/institutes-labs-centers)  
(Computational Dynamics Laboratory, Dynamics and  
Control Laboratory, and Vibrations Laboratory)  
[Balachandran, Balakumar | Department of  
Mechanical Engineering \(umd.edu\)](#)

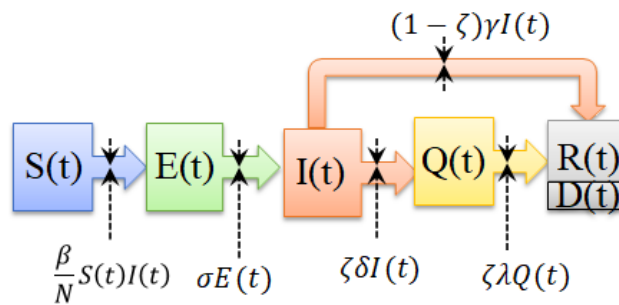
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Related Capabilities: **Statistical Modeling, Recurrent and Non-Recurrent Neural Network Models, Data-Driven Dynamics of Nonlinear Systems**

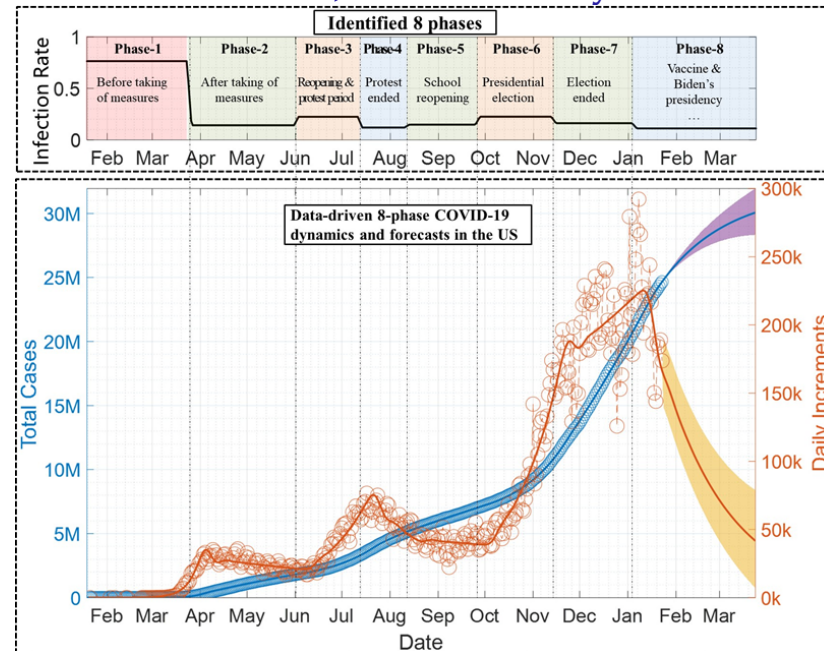
**Overall Goal of Study:** To use statistical models (Logistic Function and Generalized Logistic Function based models), physics informed neural networks, and delay dynamics-based models (improved extended compartmental models) to further our understanding of COVID-19 dynamics



Generalized Logistic Function model



Extended Compartmental Model Developed in ME@UMD



**Potential uses of study:**

- a) To make forecasts
- b) To understand the effectiveness of different measures (e.g., quarantining)

- Joint Work with Dr. Xianbo Liu and Dr. Xie Zheng, ME, UMD
- Other participants: Mr. Agustin Jauregui (sophomore) and Ms. Christina Nikiforidou (junior), ME, UMD
- Liu, X., Zheng, X., and Balachandran, B. 2020. COVID-19: data-driven dynamics, statistical and distributed delay models, and observations, *Nonlinear Dynamics*, Vol. 101, pp:1527–1543. //doi.org/10.1007/s11071-020-05863.

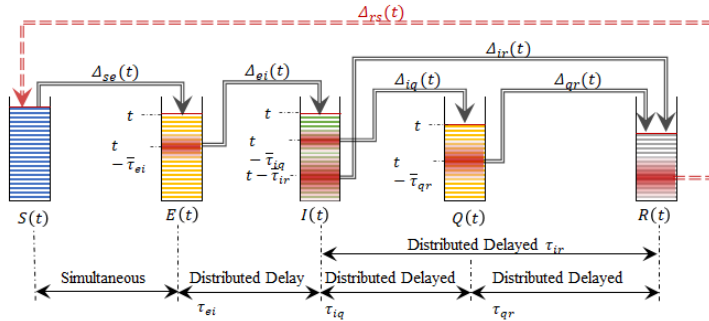
COVID-19 Data of US

Enhanced Model

Data-Driven Algorithms

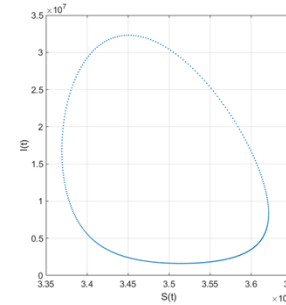
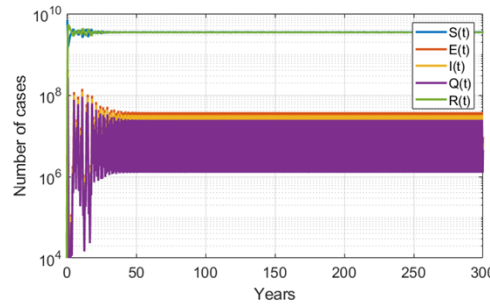
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## Long-Term Nonlinear Dynamics of COVID-19 Infection



Periodic solution : COVID-19 becomes a stable and predictable seasonal epidemic

With Parameters  $\beta_0 = 0.3$ ,  $\delta = 0.3$ ,  $\omega = 0.0005$



Consideration 1: Lost immunity from the recovered cases

$$\Delta_{rs}(t) = \omega R(t)$$

Consideration 2: Seasonal dependent infection rate [3]

$$\beta = \beta_0(1 + \delta \cos 2\pi t)$$

❖ Understanding of multi-phase and multi-scale behavior and nonlinear dynamics important for long-term forecasts

<p>P.G. County</p>	<p>MD</p>	<p>U.S.</p>	<p>World</p>
<p>Generalized logistic function based model</p> <p>Susceptible <math>S(t)</math> <math>\xrightarrow{\text{infection rate}}</math> Infectious <math>I(t)</math></p> $N \equiv S(t) + I(t)$ $I(t) = \frac{L}{(1 + e^{-k(t-t_0)})^{\frac{1}{\nu}}}$	<p>Enhanced SEIQR model with distributed delay [1]</p> <p>Compartment model with 5 state variables: S, E, I, Q, and R. The transmission periods among the 5 states follow some distribution</p>		<p>High-dimensional composite model</p> <p>❖ The sub-model can be based on the improved SEIQR model</p>